

Linear impulse and momentum

Fact —

$$\mathbf{Momentum} = \text{mass} \times \mathbf{velocity}$$

Note that since *velocity* is a vector quantity, so is momentum.

In particular, in one dimension, this means that it is important to specify a direction.

Fact —

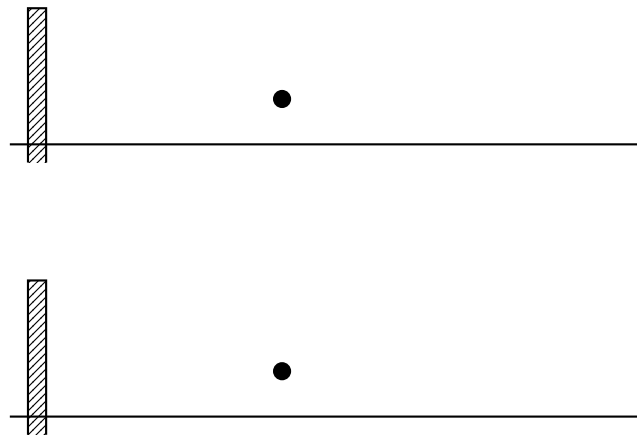
$$\mathbf{Force} = \frac{d}{dt}(\mathbf{momentum}) \quad (\text{N2})$$

$$\mathbf{Impulse} = \Delta \mathbf{momentum}$$

$$\mathbf{Impulse} = \mathbf{Force} \times \text{time}$$

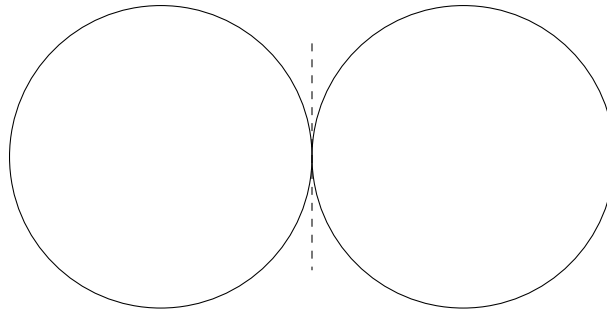
Example

A truck of mass 1400 kg moving on a straight horizontal track at 2 ms^{-1} runs into fixed buffers and rebounds at 1 ms^{-1} . The average force exerted by the buffers on the truck is 3500 N. How long were the buffers in contact with the truck?



Collisions and the Principle of Conservation of Momentum

Fact (Newton's Third Law) — Every **action** has an equal and opposite **reaction**



impulse on the left particle

impulse on the right particle

Fact (Principle of Conservation of Momentum) —

For an **isolated system**, the total momentum of the system is constant.

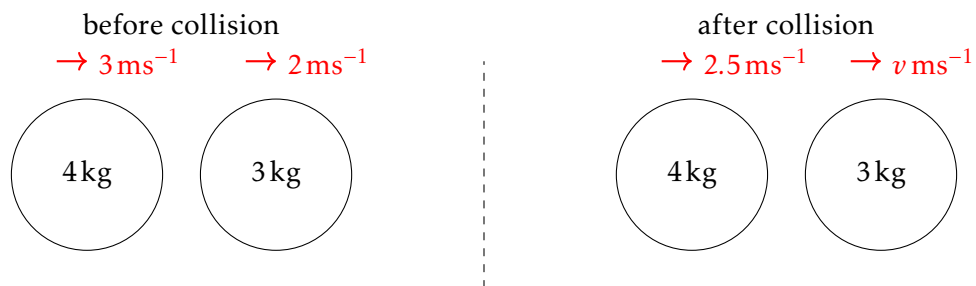
Example

A body of mass 2 kg moving on a smooth horizontal surface at 3 ms^{-1} , collides with a second body of mass 1 kg which is at rest. After the collision the bodies coalesce. Find the common speed of the bodies after impact.

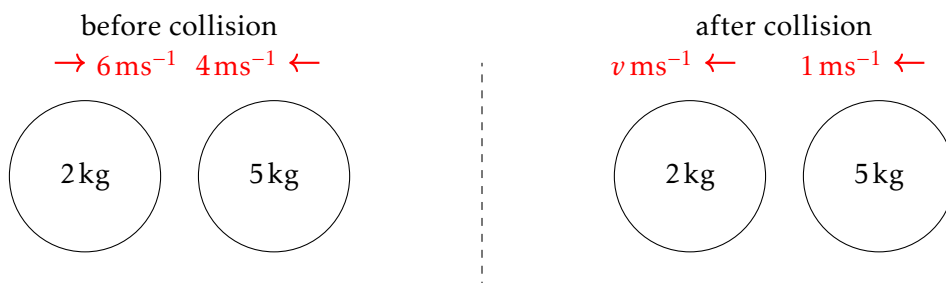


Example

The two bodies shown collide on a smooth horizontal surface. Find the value v , the speed of the lighter body after impact.

**Example**

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Example (Madas M1 Collisions Q9)

Two smooth spheres of equal radius, A and B , of mass 3 kg and $m\text{ kg}$ respectively, are moving in the same direction, along a straight line on a smooth horizontal plane. The spheres collide and the magnitude of impulse exerted on B by A is 15 N s . Before the collision, the respective speeds of A and B are 8 ms^{-1} and 2 ms^{-1} . After the collision B is moving with speed 2 ms^{-1} relative to A .

Determine the value of m and the speed of B , after the collision.

Restitution

Fact (Newton's Experimental Law / Newton's Law of Restitution) —

$$\frac{\text{speed of separation of particles}}{\text{speed of approach of particles}} = e$$

e is called the 'coefficient of restitution'

- $0 \leq e \leq 1$
- $e = 1$ - collision is perfectly elastic
- $e = 0$ - collision is perfectly inelastic

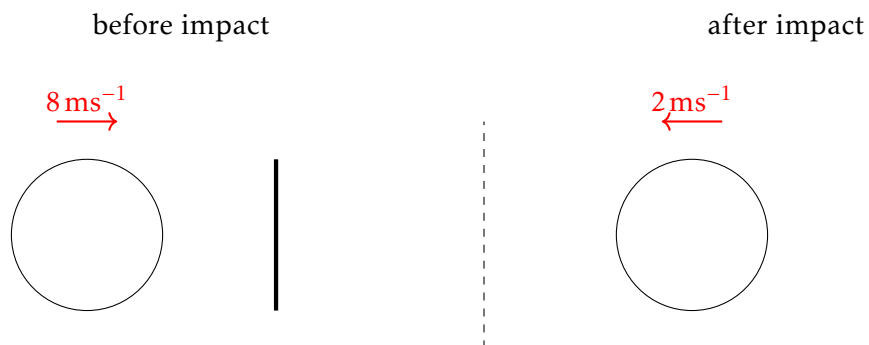
Tip (Separation is the opposite direction to approach!)

$$v_A - v_B = -e(u_A - u_B)$$

For particles with initial velocities u , and final velocities v , where the direction has been specified.

Example

A particle collides *normally* with a fixed vertical plane. The diagram shows the speeds of the particle before and after the collision. Find the value of the coefficient of restitution e



Example

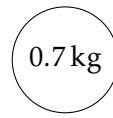
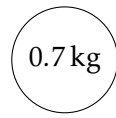
A particle falls 22.5 cm from rest onto a smooth horizontal plane. It then rebounds to a height of 10 cm. Find the coefficient of restitution between the particle and the plane. Give your answer to 2 s.f.

Example

A metal ball of mass 70 g is moving at 4 ms^{-1} . It collides with a wooden ball of mass 30 g, which is moving in the same line in the opposite direction at 6 ms^{-1} . The coefficient of restitution is 0.5. Find the speeds of the balls after the collision.

before impact

after impact

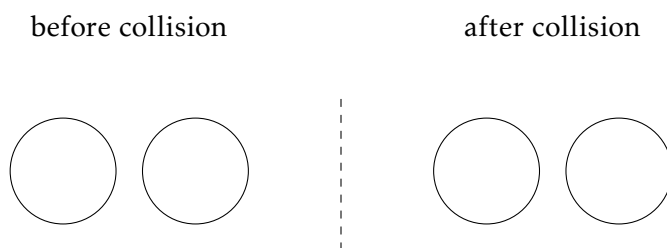


Energy in Collisions

Example

Two spheres A and B of equal radii have masses 3 kg and 5 kg respectively. A and B move towards each other along the same straight line on a smooth horizontal surface with velocities 3 ms^{-1} and 2 ms^{-1} respectively.

- If coefficient of restitution is $\frac{3}{5}$ find the velocities of the spheres after the collision.
- Find also the loss of kinetic energy due to the impact



Example

A sphere of mass 8 kg moving at 2 ms^{-1} collides with another sphere of mass 2 kg moving at 3 ms^{-1} in the opposite direction. Find, in terms of the coefficient of restitution e , the loss of kinetic energy resulting from the collision.

